



## Summary

This paper proposes the Goal-based Neural Variational Agent (GNeVA), an interpretable generative model for motion prediction with robust generalizability to out-of-distribution cases. Experiments on motion prediction datasets validate that the fitted model can be interpretable and generalizable and can achieve comparable performance to state-of-the-art results.

## Motivations

- Modeling the uncertain and multi-modal driver behaviors for motion prediction.
- Improve limited model generalizability: Performance degradation facing Out-of-Distribution (OOD) data [1].
- Improve limited model interpretability: Most state-of-the-art methods propose end-to-end black-box prediction models.

## Problem Formulation

- Observation:** Observe surroundings in the previous  $H$  time steps.
- Prediction:** Predict a target agent's future  $T$ -step trajectory.
- Environment Semantics:** The set  $\mathcal{S}$  of objects in the surroundings besides traffic participants (e.g., road geometry, traffic regulations).
- Traffic Participants:** The set  $\mathcal{P}$  of individuals or entities interacting in the current traffic (e.g., vehicles, cyclists, and pedestrians). A subset of them  $\mathcal{T}$  are targets to predict.
- Objective:** Find the optimal model  $f \in \mathcal{F}$  that parameterizes a probabilistic model that maximizes the likelihood of the target agent's future states

$$\max_{f \in \mathcal{F}} \prod_{i=1}^{|\mathcal{T}|} \prod_{t=1}^T p(\mathbf{x}_{H+t}^{(i)} | f(\mathbf{x}_{<H+t}^{(j)}, \mathbf{s}_{<H+t}^{(k)}); j \in \mathcal{P}, k \in \mathcal{S})$$

- Target-driven Motion Prediction:** Reduce the problem into two stages: first sample from a continuous spatial distribution over plausible future trajectory endpoints (i.e., goals), and then complete the intermediate trajectory [2].

## Assumptions and Design Ideas

- Multimodal Goal Distribution:** Assume the goals follow a mixture of Gaussian.
- Disentangled Conditional Posteriors for Generalization:** Assume the means and precision matrices follow a Normal-Wishart conjugate prior distribution to improve model generalizability.
  - Posterior of mean** is conditioned on the environment semantics and all other participants  $\mathbf{s}$ .
  - Posterior of precision** is only conditioned on other participants  $\mathbf{x}_{\leq H}$ .

## References

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## Variational Structure of the Spatial Distribution of Goals

The endpoint position  $g \in \mathbb{R}^2$  of a target agent's future trajectory is assumed to follow a Bayesian mixture of Gaussian distributions. As illustrated in Figure 1, we utilize an unconditional generative process in the following form with learnable prior parameters:

$$\mathbf{z} \sim \prod_{n=1}^N \prod_{c=1}^C \pi_c^{z_{nc}},$$

$$g | \mathbf{z}, \boldsymbol{\mu}, \boldsymbol{\Lambda} \sim \prod_{n=1}^N \prod_{c=1}^C \mathcal{N}(g_n | \boldsymbol{\mu}_c, \boldsymbol{\Lambda}_c^{-1})^{z_{nc}},$$

$$\boldsymbol{\mu}_c, \boldsymbol{\Lambda}_c \sim \mathcal{N}(\boldsymbol{\mu}_c | \boldsymbol{\eta}_0, (\beta_0 \boldsymbol{\Lambda}_c)^{-1}) \mathcal{W}(\boldsymbol{\Lambda}_c | V_0, \nu_0).$$

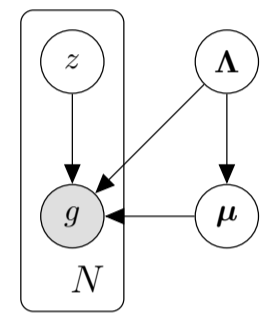


Figure 1. Likelihood Family

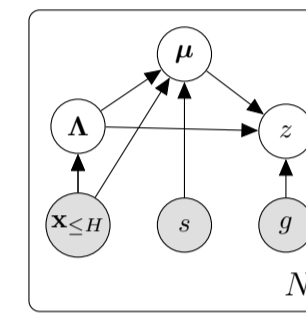


Figure 2. Variational Family

However, the mean vectors and precision matrices should be conditioned on observed history information  $\mathbf{x}_{\leq H}$  and  $\mathbf{s}$ . Therefore, we learn a set of functions to parameterize the mean-field variational distributions of  $\boldsymbol{\mu}$  and  $\boldsymbol{\Lambda}$  and evaluate the distribution of  $\mathbf{z}$  by

$$\log q(z_{nc}) \approx \mathbb{E}_{q(\boldsymbol{\mu}, \boldsymbol{\Lambda})} [\log p(g_n | \boldsymbol{\mu}_c, \boldsymbol{\Lambda}_c^{-1}, z_{nc})].$$

## Goal-based Neural Variational Agents (GNeVA)

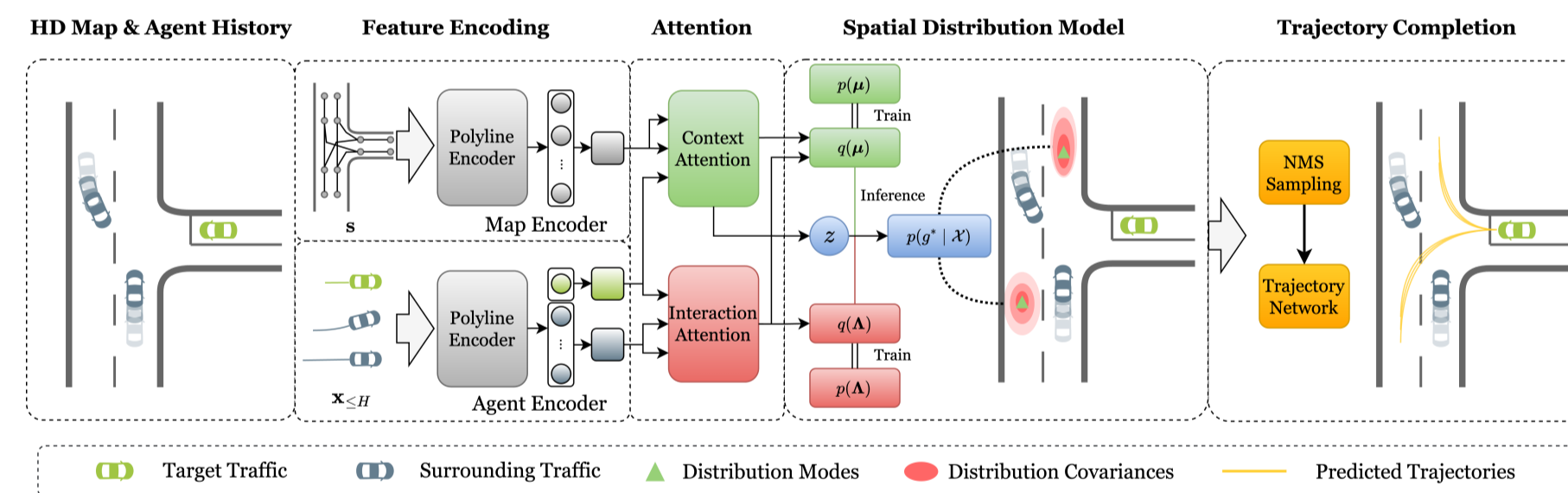


Figure 3. Overview of the GNeVA framework.

- Feature Encoding:** The traffic scenario is represented as a collection of polylines. We encode map polylines and participants' history trajectories by two separate encoders, resulting in three features: map features  $\mathbf{m}$ , target participant's history feature  $\mathbf{e}$ , and surrounding participants' history feature  $\mathbf{o}$ .
- Attention Modules** Model global interactions and parameterize the posterior distributions of  $\boldsymbol{\mu}$  and  $\boldsymbol{\Lambda}$ :
  - Context Attention** uses  $\mathbf{e}$  as query, concat  $[\mathbf{m}, \mathbf{o}]$  as key and value, and outputs parameters in  $q(\boldsymbol{\mu})$ .
  - Interaction Attention** uses  $\mathbf{e}$  as query, concat  $[\mathbf{e}, \mathbf{o}]$  as key and value, and output parameters in  $q(\boldsymbol{\Lambda})$ .
- Proxy  $z$ -posterior Network:** An additional module trained to estimate the variational posterior distribution of  $\mathbf{z}$  using history features:

$$\tilde{p}(\mathbf{z} | \mathbf{x}_{\leq H}, \mathbf{s}) = \text{MLP}(\text{concat}[\mathbf{x}_{\leq H}, \mathbf{s}]) \approx q(\mathbf{z})$$

- Sampling and Trajectory Completion:** Sample goals from the following posterior predictive Student's t-distribution using Non-Maximum Suppression

$$p(g^*) \approx \sum_{c=1}^C \tilde{p}(\mathbf{z}) \text{St}_{\nu_c-1} \left( \boldsymbol{\eta}_c, \frac{\beta_c + 1}{\beta_c (\nu_c - 1)} V_c^{-1} \right).$$

We use a cascade of MLPs for each sampled goal to complete the intermediate trajectories with the goal and the context attention module output as inputs.

## Benchmark Results

Table 1. Results on INTERACTION validation set.

	mADE <sub>6</sub>	mFDE <sub>6</sub>
DESIRE [3]	0.32	0.88
MultiPath [4]	0.30	0.99
TNT [2]	<b>0.21</b>	<b>0.67</b>
GNeVA (Ours)	<b>0.25</b>	<b>0.64</b>

Table 2. Results on Argoverse validation set.

	mADE <sub>6</sub>	mFDE <sub>6</sub>	MR <sub>6</sub>
TPCN [5]	<b>0.73</b>	1.15	0.11
mmTrans [6]	<b>0.71</b>	1.15	0.11
LaneGCN [7]	<b>0.71</b>	<b>1.08</b>	-
GNeVA (Ours)	0.78	<b>1.06</b>	<b>0.10</b>

## Generalizability Analysis

Table 3. Model Performance under Cross-scenario Tests

Validate Scenario	Train Scenario					
	Intersection		Roundabout		Full Dataset	
	mADE <sub>6</sub>	mFDE <sub>6</sub>	mADE <sub>6</sub>	mFDE <sub>6</sub>	mADE <sub>6</sub>	mFDE <sub>6</sub>
Intersection	0.56	1.41	0.56	1.39	0.31	0.73
Roundabout	0.61	1.56	0.44	1.08	0.32	0.76

Table 4. Cross Dataset Evaluation Results.

Dataset	Argoverse (validate)			INTERACTION (validate)	
	mADE <sub>6</sub>	mFDE <sub>6</sub>	MR <sub>6</sub>	mADE <sub>6</sub>	mFDE <sub>6</sub>
Argoverse (train)	0.78	1.06	0.10	0.37	0.91
INTERACTION (train)	0.92	1.34	0.15	0.25	0.64

## Visualizations on In-distribution (ID) and OOD Cases

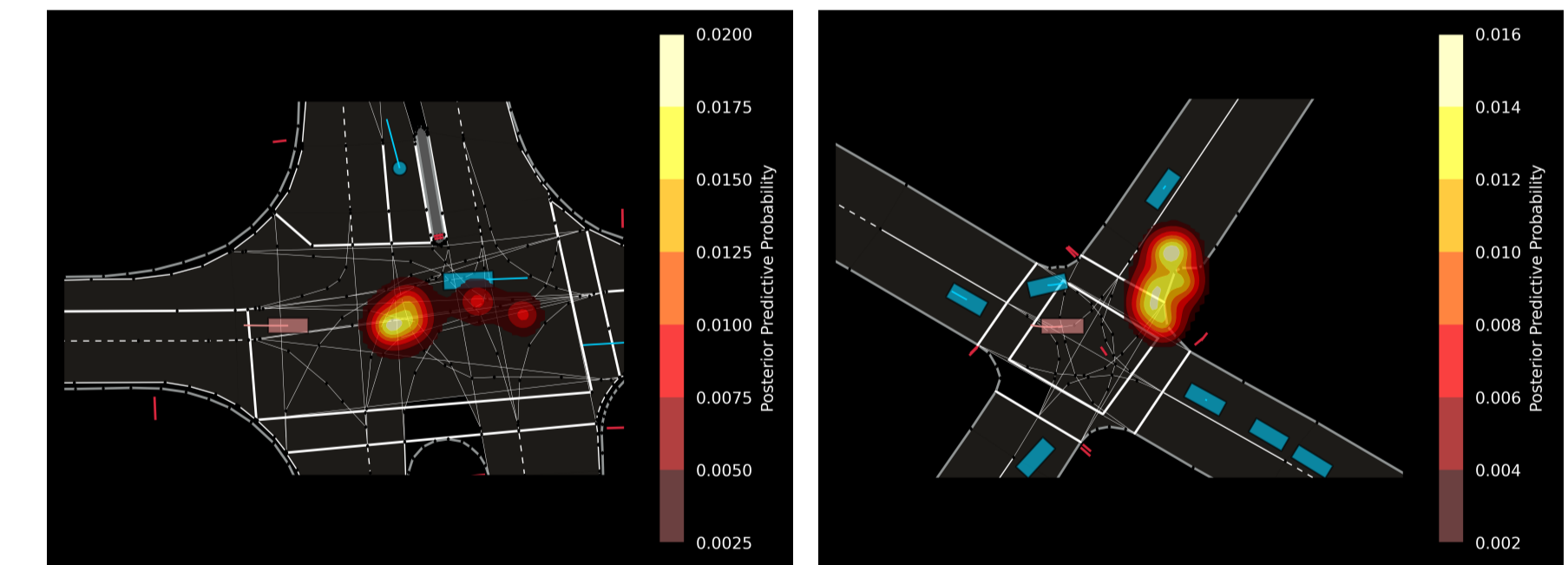


Figure 4. ID case: USA\_Intersection\_MA

Figure 5. OOD case: Intersection\_CM

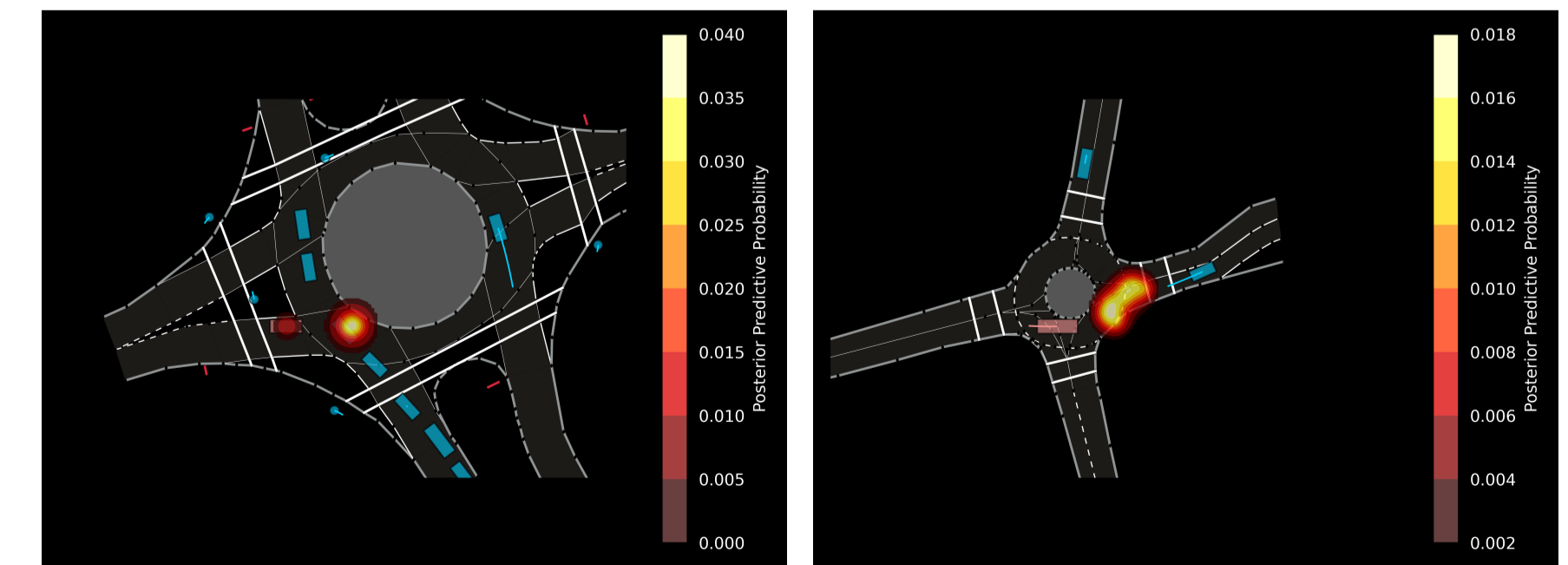


Figure 6. ID case: USA\_Roundabout\_SR

Figure 7. OOD case: Roundabout\_RW